

sem-satisfiable^{11,40}

$\vdash X \equiv_{\text{def}} \exists pr:Pgm. pr \models X$

clarification:

$\text{sem-satisfiable}(S;Pgm;X) \equiv_{\text{def}} \exists pr:Pgm. \text{sem-sat}(S;pr;X)$